IMPROVING THE DETECTION RELIABILITY OF CORRELATION-BASED WATERMARKING TECHNIQUES

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ABSTRACT

The performance of watermarking schemes based on correlation detection is closely related to the frequency characteristics of the watermark sequence. In order to improve both detection reliability and robustness against attacks, embedding of watermarks with high-frequency spectrum, in the low frequencies of the DFT domain, is introduced in this paper and theoretical analysis of correlation-based watermarking techniques with multiplicative embedding is performed. The proposed watermarking framework is successfully applied to audio signals, demonstrating its superiority with respect to both robustness and inaudibility. Experiments are conducted, in order to verify the validity of the theoretical analysis results.

1. INTRODUCTION

Watermarking technology has recently emerged as a means of copyright enforcement and content verification of multimedia data and thus, a promising tool against digital piracy. Watermarking techniques based on correlation detectors have been widely popular in the watermarking community. There has been limited effort, though, in theoretically evaluating the performance of such techniques with respect to detection reliability. In [1, 2] the statistical properties of the correlation detectors when pseudorandom watermark signals are used are explored. Research conducted so far, establishes the dependence of the system detection reliability on the frequency characteristics of the watermark signal. A theoretical performance analysis of additive embedding, correlation-based watermarking schemes using chaotic sequences is provided in [3], where the superiority of highpass skew tent chaotic watermarks against both white and lowpass watermarks, in the case of distortion-free host signals is demonstrated. High-frequency watermarks, however, are severely affected when lowpass attacks, such as compression and lowpass filtering, are imposed on the host signal.

In this paper, a watermark with highpass spectral characteristics, embedded in the low frequencies of the DFT domain is proposed. This approach guarantees that the system becomes robust to lowpass attacks while preserving its correlation properties and thus, leading to an enhancement of the detector reliability. For this purpose, piecewise-linear Markov chaotic watermarks, and in particular tent skew maps, will be employed. Their major advantage is their easily controllable spectral/correlation properties, a fact that makes them a good alternative to the widely used pseudorandom signals [3, 4]. The benefits of high-frequency watermark embedding in the low-frequency subbands of the DFT domain is established by theoretical evaluation of the statistical properties of the correlator. Theoretical performance analysis of correlation-based techniques using chaotic sequences and obeying a multiplicative rule of embedding, is also undertaken throughout this paper. It is worth noting that the proposed method is generic and can be applied on various modalities, such as images, audio and video, in combination with appropriate countermeasures for other attacks, e.g. geometric distortions. In this paper, we present a simple application of the investigated technique in watermarking of audio data.

2. DESCRIPTION OF THE WATERMARKING MODEL

Let x and X be the original signal and its Discrete Fourier Transform (DFT) coefficients, correspondingly, both of length $N_s$. Watermark embedding is performed by modifying the magnitude $F = |X|$ of the DFT coefficients, which will be considered hereafter as the host signal. Since we require that the watermark signal affects a specific low frequency subband of the host signal, it can be represented by the following formula:

$$W(n) = \begin{cases} W_o(i), & \text{if } aN_s \leq n \leq bN_s, 0 \leq i < N - 1 \\ W'_o(i), & \text{if } (1 - b)N_s \leq n \leq (1 - a)N_s, 0 \leq i < N - 1, \\ 0, & \text{otherwise} \end{cases}$$

(1)

where $n = 0, 1, \ldots, N_s - 1$ and coefficients $a, b$ ($0 < a < b \leq 0.5$) control the frequency terms that will be modified. The watermark signal $W_o$ that is used for the construction of $W$ consists of $N$ samples, where $N = [(b - a)N_s]$, and it is generated through an appropriately selected function, $W_o = g(K, N)$, where $K$ denotes the secret key, accessible only to the copyright owner or authorized users. $W_o$ is embedded in the low frequency components around coefficient 0, according to a multiplicative superposition rule. Due to the symmetry of the DFT magnitude, a reflected version of the signal $W'_o(i) = W_o(N - i)$ is also embedded in the low frequency components around coefficient $N_s - 1$. Multiplicative embedding is used since it incorporates a simple perceptual masking effect by modifying coefficients proportionally to their magnitude: $F' = F + pWF$, where $F'$ is the watermarked signal and $p$ is a constant that controls the watermark embedding power.

The correlation detector will be employed in this paper to examine whether the signal under test $F_t$ contains a watermark $W_d$ or not under a binary-decision hypothesis test framework, where the following hypotheses are considered:

- $H_0$: The test signal $F_t$ under investigation contains the watermark $W_d$, i.e., $F_t = F_o + pW_dF_o$, $F_o$ being the host signal (DFT magnitude).
• $H_1$: The test signal $F_t$ under investigation does not contain the watermark $W_d$.

Event $H_1$ can be analyzed to the events $H_{1a}$, representing the case where the test signal is not watermarked, i.e., $F_t = F_o$ and $H_{1b}$, representing the case where the test signal is watermarked with a different watermark $W_d' \neq W_d$, i.e., $F_t = F_o + pW_d F_o$. The three events $H_o$, $H_{1a}$, $H_{1b}$ mentioned above, can be combined in:

$$F_t = F_o + pW_d F_o$$

(2)

where the watermark $W_d$ is indeed embedded in the signal if $p \neq 0$ and $W_e = W_d$ (event $H_o$), and it is not embedded in the signal if $p = 0$ (no watermark is present, event $H_{1a}$) or $p \neq 0$ and $W_e = W_d' \neq W_d$ (wrong watermark presence, event $H_{1b}$).

The correlation between the signal under investigation and the watermark sequence is given by:

$$c = \frac{1}{N} \sum_{n=0}^{N-1} (F_o(n)W_d(n) + pW_e(n)F_o(n)W_d(n))$$

(3)

In order to decide on the valid hypothesis, $c$ is compared against a suitably selected threshold $T$. The performance of such a correlation-based technique can be measured in terms of the probability of false alarm $P_f(T)$ (probability of erroneously detecting the existence of a specific watermark in a signal that is not watermarked or that is watermarked with a different watermark) and the probability of false rejection $P_r(T)$ (probability of erroneously rejecting the existence of a specific watermark in a signal that is indeed watermarked) and can be graphically represented by the receiver operating characteristic (ROC) curve (plot of $P_f(T)$ versus $P_r(T)$). For the interested reader, alternative correlation-based detection schemes can be found in [5].

3. THEORETICAL PERFORMANCE ANALYSIS

To proceed with the extraction of the correlation detector statistics, we first need to make certain assumptions about the host signal. We assume that the host signal is wide-sense stationary and has a first order exponential autocorrelation function [2]:

$$R_{F_o}[k] = \mu^2 F_o + \sigma^2 F_o \beta^k, \quad k \geq 0, \quad |\beta| \leq 1$$

(4)

where $\beta$ is the parameter of the autocorrelation function and $\sigma^2 F_o$ is the host signal variance. Despite the rather simplistic assumptions, the validation of the theoretical results using numerical experiments on audio signals (Section 4), demonstrates that these assumptions hold in a great extent. In the rest of this paper, we will denote by $R_o[k]$ the $r$-th order correlation statistic of a wide-sense stationary signal $g$:

$$R_o[k_1, k_2, \ldots, k_r] = E \left[ g[n]g[n+k_1]g[n+k_2] \ldots g[n+k_r] \right]$$

(5)

We also adopt the procedure of subtracting the mean value $E[F_t]$ from the test signal $F_t$ prior to detection, for additional improvement in the detection reliability [3]. By subtracting $E[F_t]$ from the test signal we obtain the signal $F'_t$:

$$F'_t = F_t - E[F_t] = F_o' + pW_e F_o$$

(6)

where $F_o' = F_o - \mu F_o$. Obviously $\mu F_o' = 0$.

For the watermark sequences explored in this paper, the Central Limit Theorem for random variables with small dependency [6] can be used, in order to establish that the involved correlator output pdfs under the two hypotheses, $f_{e|H_o}$, $f_{e|H_1}$, attain a Gaussian distribution. Therefore, these pdfs can be described by their mean $\mu_{e|H_o}$, $\mu_{e|H_1}$, and variance values $\sigma^2_{e|H_o}$, $\sigma^2_{e|H_1}$. Using expression (3), the mean value and the variance of the correlation detector $c$, under the above assumptions, can be evaluated:

$$\mu_c = E[c] = \frac{1}{N} \left( \sum_{n=0}^{N-1} E[F_o'(n)]E[W_d(n)] \right. + \sum_{n=0}^{N-1} pE[F_0'(n)]E[W_e(n)W_d(n)] \right)$$

$$= \frac{1}{N} \sum_{n=0}^{N-1} pE[F_0'(n)]E[W_e(n)W_d(n)]$$

(7)

$$\sigma^2_c = \frac{1}{N^2} \sum_{n=0}^{N-1} \left( E[F_o'^2(n)]E[W_d^2(n)] + p^2 E[F_o'^2(n)]E[W_e^2(n)W_d^2(n)] + 2pE[F_o'(n)F_o'(m)]E[W_e(n)W_d(m)] \right.$$\n
$$+ \sum_{n=0}^{N-1} \sum_{m=0, m \neq n}^{N-1} \left( E[F_o'(n)F_o'(m)]E[W_d(n)W_d(m)] + pE[F_0'(n)F_0'(m)]E[W_e(n)W_d(m)] \right.$$\n
$$+ p^2 E[F_o'(n)F_o'(m)]E[W_e(n)W_e(m)W_d(m)] \right) - \mu_c^2$$

(8)

The above formulas are general and can be applied to all three events, $H_o$, $H_{1a}$ and $H_{1b}$. The statistical independence between the host signal $F_o$ and both watermarks $W_e$ and $W_d$ has been taken into account to derive these formulas.

The performance of the correlation-based detector depends, as we will show, on the autocorrelation and cross-correlation functions, or equivalently the power spectrum of the constructed watermarks. Therefore, functions that generate watermarks attaining desirable spectral/correlation properties are required. The controllable spectrum of certain chaotic signals has lately motivated us to use chaotic maps in watermarking schemes [3, 7], as an efficient alternative to pseudorandom watermarks. The class of the eventually expanding piecewise-linear Markov maps $\mathcal{M} : [0, 1] \to [0, 1]$, is particularly amenable to mathematical analysis [8]. The Markov sequences that will be employed hereafter, attain an exponential autocorrelation function of the form (4), where $\beta$ is an eigenvalue of the corresponding Frobenius-Perron (FP) matrix [9], which is involved in the statistics evaluation process. Zero mean chaotic watermark sequences $W_o$ can be constructed by subtracting the sequence mean value. Bearing in mind that $W_d[n] = W_e[n+k]$ according to [3] the mean value and the variance of the correlation $c$ are formulated as follows:

$$\mu_c = p \mu F_o' \left( R_x[k] - \mu_x^2 \right)$$

(9)

$$\sigma^2_c = \frac{1}{N} \left( R_x[0, k, k] - 2\mu_x R_x[0, k] + 2\mu_x^2 R_x[0] - 2\mu_x R_x[k, k] \right)$$
+ 4\mu_x^2 R_x[k] - 3\mu_x^2) p^2 R_{F_0}[0] + \frac{1}{N} (2p R_x[k, k] \\
- 4\mu_x R_x[k] + (1 - 2p \mu_x) R_x[0] + 4p \mu_x^3 - \mu_x^2) \sigma_F^2 \\
\quad + 2 N^2 \sum_{m=1}^{N-1} (N - m)(R_{F_0}[m] - \mu_{F_0}^2) R_x[m] \\
\quad + (4p \mu_x^2 - \mu_x^2) \sum_{m=1}^{N-1} (N - m)(R_{F_0}[m] - \mu_{F_0}^2) \\
\quad - \mu_x R_x[m + k] + R_x[k, k] + R_x[k + m])} \\
\quad + p \sum_{m=1}^{N-1} (N - m)(R_{F_0}[m] - \mu_{F_0}^2)(R_x[k, k, m] \\
\quad + R_x[k + m] + \sum_{m=1}^{N-1} (N - m) R_{F_0}[m] \\
\quad \{ p^2 R_x[m, k, m + k] - p^2 \mu_x (R_x[m, k, m] + R_x[m, m + k] \\
\quad + R_x[k, m + k] + R_x[k, m + k] + p^2 \mu_x^2 (2R_x[m] + 2R_x[k] \\
\quad + R_x[k, m] + R_x[k, m + k]) \\
\quad - 3p^2 \mu_x^4 \sum_{m=1}^{N-1} (N - m) R_{F_0}[m]\} - \mu_x^2, (10)

where $R[k]$ is given by (5). The above formulas involve several moments of the watermark $x$. Furthermore, by setting the watermark shift $k$ equal to zero and the embedding factor $p > 0$ expressions for the event $H_o$ can be derived. The event $H_{1a}$ can be described by an embedding factor $p$ of zero value and the event $H_{1b}$ by setting $p > 0$ and $k = 0$.

A close examination of equation (9), leads to the conclusion that the mean of the correlation detector obtains the same value for all watermarks of the same variance applied on the same host signal with a particular embedding power $p$. Therefore, the system performance is determined only by the variance of the correlation detector, which in turn is affected by the watermark spectrum. Thus, one can improve the system performance by selecting watermarks of desirable spectrum properties. High-frequency watermarks ($\beta \rightarrow 1$), which, as demonstrated in [3], lead to reduced correlation variance and, thus, improved performance when no attacks are inflicted, are indeed a good choice.

If furthermore, we restrict our attention to the class of skew tent Markov maps

$$T(x) = \left\{ \begin{array}{cl} \frac{1}{\lambda - 1} x + \frac{\lambda}{1 - \lambda}, & 0 \leq x \leq \lambda \\
\frac{1}{\lambda - 1} x + \frac{1}{1 - \lambda}, & \lambda < x \leq 1 \end{array} \right\} \quad \lambda \in (0, 1) \quad (11)$$

whose first, second and third order correlation statistics have been derived in [3], equations (9) and (10), can be modified so that they describe the two events $H_0$ and $H_{1a}$ in a more compact form:

$$\mu_c = \left\{ \begin{array}{cl} 0 & \text{p = 0 (H}_{1a}\text{)} \\\np \mu_c & \text{p = 0 (H}_o\text{)} \quad (12) \right\}$$

where $e_1, e_2$ are eigenvalues of the FP matrix $P_3$ and $\beta$ is the parameter of the host signal autocorrelation function given by (4).

Using the derived statistics for the correlator output, theoretical expressions for the ROC curves can be constructed.

4. EXPERIMENTAL RESULTS

The first set of experiments aimed at verifying the validity of the theoretical results derived throughout this paper. The proposed watermarking model was incorporated in a simple audio watermarking scheme. A music mono audio signal, of approximately 5.94 sec duration, sampled at 44.1 KHz with 16 bits per sample ($N = 262144$) was fed to the system. The host signal (DFT coefficients) was assumed to comply with the signal model of (4). The parameter $\beta$ for the specific audio signal was estimated equal to 0.95, using Mean Square Error minimization between the model autocorrelation function and the test signal autocorrelation function. The skew tent map parameter $\lambda$ was chosen to be equal to 0.3, thus leading to watermarks of highpass spectral characteristics. All sets of experiments were conducted using a total number of 10000 keys. The watermarks were embedded in the low frequency subband defined by $a = 0.01$, $b = 0.11$ and an embedding factor $p = 0.27$ was used, which produced a watermarked signal with $\text{SNR} = 23.1$ dB. ROC curve evaluation for this specific experiment, was performed for the event $H_{1a}$, corresponding to the signal not being watermarked ($p = 0$). Figure 1 demonstrates the close resemblance of the theoretical ROC curve evaluated using (12),(13) with the one evaluated experimentally. The small divergence that can be observed, can be attributed to the fact that the real audio signal is discrete-valued (quantized), as well as to the assumption made for its autocorrelation function (4). Multiple experiments involving different audio signals also verified the validity of the theoretical results.

A large number of experiments were performed to investigate the robustness of the proposed watermarking scheme to lowpass attacks and compare its performance with the performance of two alternative techniques: a) a scheme involving white pseudorandom watermark sequences ($u(i) \in \{\{-1, 1\})$) multiplicatively embedded in the same low frequency subband ($a = 0.01$, $b = 0.11$) of the DFT domain, producing watermarked signals with $\text{SNR} = 23$ dB; b) a scheme based on the time-domain audio watermarking technique presented in [10], which involves watermark modulation according to the amplitudes of the original audio samples and filtering with a lowpass Hamming filter of 25th-order with cut-off frequency of 2205 Hz, in order to improve imperceptibility and robustness to lowpass attacks. The SNR value of the watermarked
5. CONCLUSIONS

The use of high-frequency spectrum watermarks generated by chaotic sequences and embedded in the low-frequency subband of the DFT coefficients is proposed in this paper. The proposed technique guarantees improved system detection reliability, imperceptibility and robustness to lowpass attacks. Theoretical analysis of the correlation detector is being performed and closed-form expressions are derived for the correlation detector statistics of skew tent chaotic watermarks. Various sets of experiments, on a simple audio watermarking application, verify the validity of the theoretical results and demonstrate the robustness of the proposed scheme to common lowpass attacks, such as MPEG compression and mean or median filtering.

6. REFERENCES